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Assessment of theoretical procedures for hydrogen-atom abstraction by chlorine, and related reactions

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Abstract We have examined a number of hydrogenabstraction reactions and assessed various theoretical procedures with regard to their performance for geometry optimization and for calculating barriers and reaction energies. We find that the BH&H-LYP and M05-2X procedures with the 6-31+G(d,p) basis set provide reasonable predictions for the geometries of the transition structures and also yield reasonable imaginary frequencies when compared with our benchmark QCISD/6-31+G(d,p) and CCSD(T)/6-311+G(3df,2p) values. For the calculation of barriers and reaction energies, M05-2X appears to be the most accurate of the hybrid functionals. The double-hybrid functionals, B2K-PLYP, UB2-PLYP-09, ROB2-PLYP, and DSD-B-LYP-D3, when used in combination with an augmented triple-zeta basis set, give very good agreement with the benchmark URCCSD(T)/aug-cc-pVQZ energies. We find that for wavefunction procedures, use of CCSD(T) in combination with an augmented triple-zeta quality basis set is required for the accurate prediction of barriers and reaction energies for these reactions.

Dedicated to Professor Shigeru Nagase on the occasion of his 65th birthday and published as part of the Nagase Festschrift Issue.

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B. Chan e-mail: chan_b@chem.usyd.edu.au **Keywords** Hydrogen abstraction · Ab initio · Density functional theory

1 Introduction

Free radical chlorination is an important reaction in organic synthesis [1], industrial processes [2], and stratospheric chemistry [3–6]. The reaction is used for the industrial synthesis of chloroform, dichloromethane, and hexachlorobutadiene [2]. It also represents a significant loss channel for stratospheric methane, which impacts greenhouse-gas models [4]. Furthermore, radical chlorination reactions of methane and ethane are widely used as reference reactions in relative rate studies [7–12]. Finally, hydrogen-atom abstraction by chlorine is an important step for the propagation of free radical chlorination [1]. Thus, determination of accurate kinetic parameters for these types of reactions is desirable.

Computational quantum chemistry [13–15] is a powerful tool for obtaining such quantities. For instance, Yamataka and Nagase investigated hydrogen-abstraction reactions using the MP2 procedure [16]. The higher-level CCSD(T) procedure with the Dunning quadruple-zeta augcc-pVQZ basis set [17–19] has been applied to the Cl • + CH₄ \rightarrow ClH + •CH₃ reaction [20], while the related F • + CH₄ \rightarrow FH + •CH₃ reaction has been studied at the CCSD(T) level with the larger aug-cc-pCV5Z basis set [21]. Although the high-level CCSD(T) method allows the evaluation of thermodynamic and kinetic parameters with sub-kJ mol⁻¹ accuracy, it is applicable today only to relatively small systems. As a result, finding a compromise between accuracy and computational cost is important for further advancing the theoretical study of these reactions.

Taylor et al. [22] have recently examined hydrogen abstraction by chlorine atom from a set of small molecules

related to the building blocks of amino acids. It was found that for geometry optimization, some popular density functional theory (DFT) methods such as B3-LYP [23–25] and BMK [26] do not give reliable transition structures (TSs) compared with benchmark CCSD(T) or QCISD geometries. For the evaluation of energies, the theoretical procedures performed in the order W1' [27–29] > G3X (MP2)-RAD [30] > ROMP2/G3XLarge [31] ~ UB2-PLYP [32]/G3XLarge > UBMK/G3XLarge > UB3-LYP/G3XLarge.

While these results provide helpful insights into the appropriate theoretical procedures for studying hydrogen abstraction by chlorine, it would be useful to extend this study. Specifically, identifying a reliable DFT procedure for optimizing transition structures would be beneficial, because the use of CCSD(T) and QCISD geometries can rapidly become prohibitively expensive. Furthermore, it would also be attractive to evaluate the performance of a wider range of DFT procedures for the calculation of reaction energies and barriers, in the hope of further reducing the cost of computations. In the present study, we address these issues with an extended investigation into hydrogen abstraction by chlorine, and related reactions.

2 Computational details

Standard ab initio molecular orbital theory and DFT calculations were carried out with GAUSSIAN 09 [33] and MOLPRO 2006 [34]. The frozen-core approximation was used in all wavefunction correlation calculations. Geometries of stationary points were optimized using UQCISD and various DFT procedures with the 6-31+G(d,p) basis set. The DFT procedures that have been examined for their performance for geometry optimization are hybrid functionals, namely B3-LYP [23], B3-P86 [35], B3-PW91 [36], B97-2 [37], B98 [38], BH&H-LYP [39], BMK [26], M05 [40], M05-2X [41], M06 [42], M06-2X [42], MPW1PW91 [43], and PBE1-PBE [44]. Following each geometry optimization, harmonic frequency analysis at the same level of theory was carried out to confirm the nature of the stationary point as a minimum (equilibrium structure) or firstorder saddle point (transition structure).

Benchmark energies were calculated at the UR-CCSD(T)/aug-cc-pVQZ level. We employed the aug-cc-pwCVQZ basis set [45] for bromine, in place of aug-cc-pVQZ, in order to appropriately account for the correlation effects of the 3d orbitals. In the present study, we have assessed the performance of the wavefunction methods HF, MP2, MP3, MP4, CCSD and CCSD(T), as well as various DFT procedures. The DFT procedures examined include pure functionals B-LYP [23] and M06-L [42], hybrid functionals B3-LYP, LC-B-LYP [46], CAM-B3-LYP [47],

ωB97X-D [48], BH&H-LYP, BMK, M05, M05-2X, M06 and M06-2X, and double-hybrid functionals UB2-PLYP [32], UB2K-PLYP [49], and their R variants (RB2-PLYP and RB2K-PLYP) in which the proportion of HF exchange and MP2 correlation are assumed to be the same as for the U methods. In addition, we have examined UB2-PLYP-09 [50] and ROB2-PLYP [50], in which the proportion of HF exchange and MP2 correlation have been optimized using the same test set, specifically the 148 heats of formation from the G2/97 set [51, 52], as well as DSD-B-LYP-D3 [53]. Single-point energies at the above levels were calculated in combination with a variety of basis sets, including the Pople-type basis sets [13] 6-31G(d), 6-31+G(d,p), 6-311+G(2df,p), 6-311+G(3df,2p)and G3LargeXP [54], and the Dunning sets [17] cc-pVnZ and aug-cc-pVnZ (n = D, T and Q). Bond lengths reported in the paper are in Å, while relative energies are vibrationless values in kJ mol⁻¹.

3 Results and discussion

3.1 Choice of geometry

In order to identify the appropriate DFT procedure for geometry optimization, we have considered the transition structures for the set of five hydrogen-abstraction reactions that have also been used for this purpose in reference [22]:

$$Cl \bullet + CH_4 \to ClH + \bullet CH_3$$
 (1)

$$Cl \bullet + CH_3NH_3^+ \to ClH + \bullet CH_2NH_3^+$$
 (2)

 $Cl \bullet + CH_3CHO \rightarrow ClH + \bullet CH_2CHO$ (3)

$$Cl \bullet + CH_3CO_2H \rightarrow ClH + \bullet CH_2CO_2H$$
 (4)

$$\operatorname{Cl} \bullet + \operatorname{CH}_3\operatorname{CO}_2^- \to \operatorname{ClH} + \bullet \operatorname{CH}_2\operatorname{CO}_2^-$$
 (5)

We first examine the geometries obtained with the complete set of 13 hybrid DFT procedures for reaction 1, with a focus on the key bond lengths, namely the Cl–H bond that is being formed, the H–C bond that is being broken, and the distance between the Cl and C atoms. We then further assess several of the more promising procedures for reactions 2–5. We also compare the calculated imaginary frequencies with the benchmark values to assess the ability of the DFT procedures to obtain reliable estimates of the curvature on the potential energy surface in the vicinity of the transition structure. The results are shown in Table 1.

For the transition structure for the reaction of Cl• with CH₄, there is a range of 0.089 Å for the predicted Cl····H distance, with the shortest distance being the one obtained with B3-P86 (1.370 Å) and the longest being that for M05 (1.459 Å). We find that the BH&H-LYP functional

Table 1 Imaginary frequencies (ω_i , cm⁻¹) for the transition structures, and selected interatomic distances (Å), and their mean absolute deviations (MAD) and largest deviations (LD) from CCSD(T) or QCISD values

	Substrate	Method ^a	$\omega_{\rm i}$	$Cl\cdots H$	$H \cdots C$	$Cl \cdots C$	MAD	LD		
(1)	CH_4	B3-LYP	338.7	1.391	1.584	2.975	0.113	0.170		
		B3-P86	196.7	1.370	1.626	2.996	0.141	0.212		
		B3-PW91	283.7	1.383	1.584	2.968	0.113	0.170		
		B97-2	312.9	1.381	1.577	2.957	0.108	0.163		
		B98	194.9	1.373	1.646	3.020	0.155	0.232		
		BH&H-LYP	972.7	1.426	1.450	2.876	0.024	0.036		
		BMK	328.3	1.394	1.591	2.985	0.118	0.177		
		M05	761.0	1.459	1.403	2.862	0.013	0.020		
		M05-2X	807.8	1.426	1.470	2.896	0.037	0.056		
		M06	508.6	1.421	1.499	2.920	0.056	0.085		
		M06-2X	745.9	1.409	1.508	2.917	0.062	0.094		
		MPW1-PW91	356.9	1.391	1.546	2.937	0.088	0.132		
		PBE1-PBE	311.5	1.386	1.561	2.946	0.097	0.147		
		QCISD	1,254.6	1.435	1.415	2.850	0.003	-0.004		
		QCISD ^b	1,220.6	1.448	1.396	2.844	0.012	-0.018		
		CCSD(T) ^b	1,245.8	1.439	1.414	2.854				
(2)	CH ₃ NH ₃ ⁺	B3-LYP	847.0	1.391	1.550	2.868	0.051	0.170 0.212 0.170 0.163 0.232 0.036 0.177 0.020 0.056 0.085 0.094 0.132 0.147 -0.004 -0.018 0.087 0.010 0.014 0.015 0.052 0.057 0.047 0.015 -0.300 0.029 0.028 0.016 0.029 0.028 0.016 0.029 0.028 0.016 0.029 0.028 0.016 0.055 0.019 0.026 0.036 0.036		
		BH&H-LYP	1,350.6	1.402	1.473	2.819	0.005	0.010		
		M05	913.4	1.416	1.457	2.814	0.007	0.014		
		M05-2X	1,277.5	1.409	1.478	2.805	0.010	0.015		
		M06	1,030.1	1.406	1.515	2.823	0.022	0.052		
		M06-2X	1,206.7	1.393	1.520	2.823	0.025	0.057		
		QCISD	1,536.4	1.402	1.463	2.814				
(3)	CH ₃ CHO	B3-LYP	1,068.5	1.480	1.393	2.868	0.029	0.047		
		BH&H-LYP	1,442.1	1.495	1.341	2.834	0.009	0.015		
		M05	1,216.1	1.180	1.295	2.831	0.119	-0.300		
		M05-2X	1,139.6	1.509	1.340	2.842	0.017	0.029		
		M06	1,075.2	1.508	1.342	2.847	0.018	0.028		
		M06-2X	1,096.5	1.485	1.358	2.842	0.011	0.016		
		QCISD	1,612.0	1.480	1.346	2.826				
(4)	CH ₃ CO ₂ H	B3LYP	998.4	1.453	1.429	2.880	0.041	6 0.085 2 0.094 8 0.132 7 0.147 3 -0.004 2 -0.018 1 0.087 5 0.010 7 0.014 0 0.015 2 0.052 5 0.057 9 0.047 9 0.047 9 0.047 9 0.015 9 -0.300 7 0.029 8 0.028 1 0.062 7 0.010 6 0.055 3 0.019 7 0.026 4 0.036 2 0.498 5 0.115		
		BH&H-LYP	1,425.1	1.468	1.372	2.838	0.007	0.010		
		M05	1,257.8	1.516	1.314	2.829	0.036	0.055		
		M05-2X	1,227.6	1.474	1.374	2.847	0.013	0.019		
		M06	931.9	1.477	1.377	2.854	0.017	0.026		
		M06-2X	1,085.3	1.451	1.403	2.854	0.024	0.036		
		QCISD	1,581.6	1.461	1.367	2.828				
(5)	$CH_3CO_2^-$	B3-LYP	294.7	1.340	2.041	3.308	0.312	0.498		
		BH&H-LYP	203.0	1.379	1.658	3.020	0.075	0.115		
		M05	172.4	1.330	1.985	3.264	0.282	0.442		
		M05-2X	108.8	1.337	1.895	3.184	0.223	0.352		
		M06	186.9	1.347	1.910	3.210	0.233	0.367		
		M06-2X	226.4	1.360	1.773	3.106	0.149	0.230		
		QCISD	422.5	1.415	1.543	2.945				

Benchmark CCSD(T) and QCISD values obtained from Ref. [22]

^a The 6-31+G(d,p) basis set was employed unless otherwise noted

^b 6-311+G(3df,2p)

(1.426 Å) yields the best agreement with the benchmark CCSD(T) value (1.439 Å). The range for the calculated $H \cdots C$ distance is much wider (0.243 Å), from 1.403 Å for M05 to 1.646 Å for B98. In this case, the M05 procedure gives the best agreement with the CCSD(T) value of 1.414 Å. The range for the Cl \cdots C distance (0.176 Å) is somewhat smaller than that for the $H \cdots C$ distance (0.243 Å), indicating some compensation between Cl \cdots H and $H \cdots C$ bonds. Overall, we find that the BH&H-LYP, M05-2X, and M05 procedures provide the best estimates for the key bond lengths in the Cl \bullet + CH₄ transition structure, with mean absolute deviations (MADs) of 0.024, 0.037, and 0.013 Å, respectively.

For the calculated imaginary frequencies for the TSs for the reaction of Cl• with CH₄, we find that when compared with the CCSD(T) value of 1,245.8 cm⁻¹, all DFT procedures underestimate the frequency of this vibration, with a lowest value of 194.9 cm⁻¹ predicted by B98. We find that BH&H-LYP, M05-2X, and M05 yield frequencies that are in closest agreement with CCSD(T), with values of 971.8, 807.8, and 761.0 cm⁻¹, respectively. The closer agreement of these three DFT procedures with CCSD(T) results, both in terms of the key bond distances, as well as the predicted imaginary frequencies, has led us to further investigate their performance for reactions 2–5. We have also included in our analysis the widely used B3-LYP method and two procedures closely related to M05 and M05-2X, namely M06 and M06-2X.

We find that these functionals generally give MADs for the transition structures for reactions 2-5 that are smaller than 0.05 Å, with the exception of those for reaction 5, for which all the DFT procedures appear to significantly overestimate the $Cl \cdots C$ separation. For example, the MAD for BH&H-LYP is 0.075 Å, while much larger deviations are seen for B3-LYP (0.312 Å), M05 (0.282 Å), M05-2X (0.223 Å), M06 (0.233 Å), and M06-2X (0.149 Å). For reactions 2–5, BH&H-LYP has the smallest overall MAD (0.024 Å) as well as the smallest LD (largest deviation, 0.115 Å), while B3-LYP yields the largest MAD (0.109 Å) and LD (0.498 Å) values. It is also apparent that BH&H-LYP gives the closest agreement with QCISD for the calculated imaginary frequencies for reactions 2-5. Based on these observations, we have chosen BH&H-LYP/ 6-31+G(d,p) for geometry optimization for the rest of our investigation.

3.2 Choice of single-point energy

Turning our attention to the performance of the various procedures for calculating relative energies, we have investigated the prototypical hydrogen-atom abstractions from CH_4 by the Cl•, F•, Br•, HO•, and HOO• radicals, and abstraction from CH_3CHO by Cl•:

$$Cl \bullet + CH_4 \to ClH + \bullet CH_3$$
 (1)

$$\mathbf{F} \bullet + \mathbf{C}\mathbf{H}_4 \to \mathbf{F}\mathbf{H} + \bullet \mathbf{C}\mathbf{H}_3 \tag{6}$$

$$Br \bullet + CH_4 \to BrH + \bullet CH_3 \tag{7}$$

$$\mathrm{HO} \bullet + \mathrm{CH}_4 \to \mathrm{H}_2\mathrm{O} + \bullet \mathrm{CH}_3 \tag{8}$$

$$HOO \bullet + CH_4 \to H_2O_2 + \bullet CH_3 \tag{9}$$

$$Cl \bullet + CH_3CHO \rightarrow ClH + \bullet CH_2CHO$$
 (10)

Reaction 10 was included in the present study because it represents the most challenging case examined in reference 22, largely associated with spin contamination in the TS for abstraction, and in the product \bullet CH₂CHO radical.

We have probed the performance of the high-level CCSD(T) procedure by comparing several calculated bond dissociation energies (BDEs) relevant to reactions 1 and 6-9, and the corresponding reaction energies, with experimental values (Table 2). It can be seen that UCCSD(T) and URCCSD(T) give BDEs and reaction energies (ΔE_r) that are very close to one another. In general, the use of the aug-cc-pVQZ basis set yields BDEs that are in good accord with experimental values, with an MAD of 1.7 kJ mol^{-1} . The agreement is somewhat less good when the smaller aug-cc-pVTZ basis set is used, with an MAD for the BDEs of 7.1 kJ mol⁻¹. For the energies of reactions 1 and 6–9, better results are obtained with both basis sets, with MADs of 3.2 and 1.0 kJ mol⁻¹, respectively, for the TZ and OZ basis sets. On the basis of these results, we have chosen URCCSD(T)/aug-cc-pVQZ as the benchmark method. While the aim of the present study was assessment of theoretical procedures, we provide relevant URCCSD(T)/ aug-cc-pVQZ barriers and reaction energies in Table 3.

We have surveyed a variety of DFT- and wavefunctionbased methods and compared the calculated vibrationless barriers and reaction energies with the benchmark UR-CCSD(T)/aug-cc-pVQZ values. The MADs for the barriers and reaction energies are presented in Tables 4 and 5, respectively. First, we examine the performance of the various methods in predicting barriers. It is apparent that with the exception of B-LYP, all DFT procedures examined have MADs that are less than 10 kJ mol⁻¹ for at least some of the basis sets. Among these, M06-2X is the only one that achieves such accuracy in combination with all the basis sets examined. We also note that LC-B-LYP and BMK give MADs that are less than 10 kJ mol⁻¹ for all basis sets other than 6-31G(d), while CAM-B3-LYP and M05-2X have MADs that are less than 10 kJ mol⁻¹ except with the aug-cc-pVDZ basis set. When we further examine the basis set effect among the DFT methods, we do not find consistent improvement as the basis set size increases. In particular, for M06-L, B3-LYP, ω B97X-D, M05, and M06, the best results are actually obtained with the smallest 6-31G(d) basis set.

	UCCSD(T) AVTZ ^a	URCCSD(T) AVTZ ^a	UCCSD(T) AVOZ ^a	URCCSD(T) AVOZ ^a	Expt ^b
	AVIL	AVIZ	RVQL	AVQL	
CH ₃ –H	465.9	465.9	468.5	468.5	470.4
Cl–H	439.0	439.0	444.9	445.0	445.3
F–H	582.6	582.7	589.5	589.6	591.2
Br–H	384.1	384.3	392.1 ^c	392.1 ^c	392.8
HO–H	516.5	516.6	522.5	522.6	525.4
НОО–Н	387.0	387.0	390.2	390.2	393.1
MAD	7.2	7.1	1.7	1.7	
$\Delta E_{\rm r}$ 1	26.9	26.9	23.6	23.5	25.0
$\Delta E_{\rm r}$ 6	-116.7	-116.8	-121.0	-121.1	-120.8
$\Delta E_{\rm r}$ 7	81.8	81.6	76.4 ^c	76.5 ^c	77.6
$\Delta E_{\rm r}$ 8	-50.6	-50.7	-54.0	-54.1	-55.1
$\Delta E_{\rm r}$ 9	78.9	78.9	78.3	78.3	77.3
MAD	3.3	3.2	1.0	1.0	

Table 2 Comparison of calculated and experimental bond dissociation energies (BDEs), and the energies (ΔE_r) of related hydrogen-atomtransfer reactions 1 and 6–9, as well as the corresponding mean absolute deviations (MADs) (vibrationless, kJ mol⁻¹)

^a AVnZ = aug-cc-pVnZ (n = T, Q)

^b Obtained from NIST Chemistry Webbook [58] and back-corrected to vibrationless values using zero-point vibrational energies and thermal corrections to enthalpies obtained from scaled [59] BH&H-LYP/6-31+G(d,p) frequencies

^c The aug-cc-pwCVQZ basis set was used for Br

Table 3 URCCSD(T)/aug-cc-pVQZ//BH&H-LYP/6-31+G(d,p) vibrationless and 0 K barriers (E^{\ddagger}) and reaction energies (ΔE_r) for reactions 1 and 6–10 (kJ mol⁻¹)

Reactants		Vibrationless		0 K		
		$\overline{E^{\ddagger}}$	$\Delta E_{ m r}$	$\overline{E^{\ddagger}}$	$\Delta E_{\rm r}$	
F∙	CH_4	0.3	-121.1	-4.8	-135.4	
Cl●	CH_4	29.7	23.5	12.9	2.4	
Br● ^a	CH_4	70.2	76.5	53.0	53.5	
НО∙	CH_4	24.9	-54.1	18.4	-59.3	
HOO●	CH_4	112.3	78.3	103.4	72.0	
Cl●	CH ₃ CHO	21.7	-18.1	5.0	-34.3	

^a The aug-cc-pwCVQZ basis set was used for Br

We now turn our attention to the two double-hybrid functionals B2-PLYP and B2K-PLYP, with both U and R formulations. They represent two "extremes" among the double hybrids that are based on B-LYP. Thus, B2-PLYP includes the least amount of ab initio components (53% HF and 27% MP2), while B2K-PLYP includes 72% HF and 42% MP2, which is the most among the B2x-PLYP family of double-hybrid procedures. We find that the performance of B2K-PLYP is rather sensitive to the size of the basis set, where small basis sets lead to fairly poor results. On the other hand, the performance of B2-PLYP appears to be somewhat less sensitive to basis set size.

This is consistent with the proportion of DFT and wavefunction contributions in these two double hybrids, such that B2K-PLYP behaves more like a wavefunction method, in which the use of an adequately sized basis set is critical, while the performance of B2-PLYP deteriorates less with decreasing basis set size, as is often the case with DFT procedures. As a result of these basis set considerations, we find that when used in combination with small basis sets, B2-PLYP provides somewhat more reliable barriers. However, as the size of the basis set increases, B2K-PLYP eventually outperforms B2-PLYP.

The UB2-PLYP-09 method contains 62% HF and 35% MP2, while ROB2-PLYP contains 59% HF and 28% MP2. Thus, they lie between B2-PLYP and B2K-PLYP in terms of wavefunction contribution to energies. We find that for the most part, their performance also lies between the two extremes. We also note that, in general, the U and R formalisms yield comparable results for these double-hybrid procedures. The DSD-B-LYP-D3 procedure is a new type of double-hybrid functional that makes use of SCS-MP2 [55]

Table 4 Mean absolute deviations from URCCSD(T)/AVQZ^a benchmark values for vibrationless barriers (kJ mol⁻¹) for reactions 1 and 6–10^b

	B1	B2	B3	B4	LXP	VDZ	VTZ	VQZ	AVDZ	AVTZ	AVQZ
Pure DFT methods											
B-LYP	20.4	30.0	29.5	31.0	30.4	31.5	28.6	29.5	35.2	30.1	29.9
M06-L	9.5	16.7	16.4	17.4	16.5	16.9	15.9	14.5	21.3	16.8	15.8
Hybrid DFT metho	ds										
B3-LYP	7.2	13.1	13.3	14.8	14.1	14.4	12.5	13.2	18.4	13.8	13.6
LC-B-LYP	12.9	9.5	8.4	8.0	8.2	8.2	8.4	8.4	9.0	8.3	8.3
CAM-B3-LYP	8.8	7.8	8.0	9.3	8.5	8.5	7.5	8.0	12.1	8.3	8.1
ωB97X-D	5.7	8.8	9.5	11.1	10.4	9.1	8.2	8.6	14.3	9.6	9.0
BH&H-LYP	21.3	11.8	11.3	9.8	10.7	10.5	11.8	11.3	6.9	10.9	11.1
ВМК	10.1	4.6	7.7	8.7	8.0	6.9	7.1	7.1	8.4	7.8	7.5
M05	8.7	10.0	13.0	13.6	13.3	11.3	10.0	11.0	14.9	11.0	11.3
M05-2X	6.0	5.1	4.6	6.6	6.2	4.8	5.3	5.5	10.1	6.9	6.0
M06	7.3	9.0	10.8	12.2	11.5	11.7	9.3	8.6	14.5	10.3	9.3
M06-2X	9.0	3.1	5.0	6.3	5.5	4.8	5.0	4.8	7.1	5.8	5.1
Double-hybrid DFT	r methods										
UB2-PLYP	13.4	6.0	4.5	6.0	5.3	3.0	3.9	4.9	7.9	5.8	5.7
UB2K-PLYP	23.6	11.1	5.6	3.4	4.1	10.7	6.1	3.9	1.4	2.1	2.2
RB2-PLYP	15.2	6.3	3.7	5.4	4.6	3.5	3.3	4.3	6.3	5.3	6.0
RB2K-PLYP	25.7	12.8	6.7	4.1	5.2	12.7	7.0	4.6	3.3	3.3	2.5
UB2-PLYP-09	17.7	6.4	2.6	3.3	2.8	5.0	2.5	2.3	4.5	3.2	3.3
ROB2-PLYP	20.6	8.3	3.5	2.0	2.8	8.1	4.0	2.2	1.6	1.6	3.4
DSD-B-LYP-D3	20.3	7.6	2.2	2.0	1.7	7.4	3.0	1.6	3.2	2.5	2.4
Unrestricted wavefu	unction me	thods									
UHF	71.7	62.1	61.9	60.6	61.8	61.5	62.3	62.4	57.9	61.9	62.3
UMP2	36.7	23.2	14.0	11.8	12.4	21.5	13.7	10.6	10.6	10.0	9.5
UMP3	41.6	28.7	20.5	18.3	19.1	27.6	19.7	16.0	13.6	14.4	13.6
UMP4	38.0	23.0	13.3	10.5	11.3	22.8	12.5	8.6	8.9	8.1	6.1
UCCSD	36.8	23.1	16.6	14.3	15.3	22.9	16.2	12.7	8.6	10.8	10.0
UCCSD(T)	32.8	17.7	9.1	6.0	6.9	17.9	8.3	3.7	2.5	2.2	0.5
Restricted-open-she	ell wavefun	ction meth	ods								
RHF	86.9	76.6	74.6	73.2	74.1	76.1	75.0	74.7	71.6	74.2	74.6
RMP2	28.8	19.1	9.6	9.0	8.9	15.6	9.3	9.0	9.2	9.7	9.7
RMP3	39.8	27.4	19.2	17.0	17.9	26.2	18.5	14.6	12.2	13.2	12.3
RMP4	34.7	19.4	10.2	7.7	8.5	19.7	9.6	5.6	6.2	5.4	4.0
URCCSD	37.3	23.7	17.1	14.8	15.8	23.4	16.7	13.1	9.1	11.3	10.5
URCCSD(T)	32.5	17.4	8.6	5.5	6.4	17.6	7.8	3.3	2.3	1.8	0.0

^a The aug-cc-pwCVQZ basis set was employed for bromine

^b B1 = 6-31G(d), B2 = 6-31+G(d,p), B3 = 6-311+G(2df,p), B4 = 6-311+G(3df,2p), LXP = G3LargeXP, VnZ = cc-pVnZ, AVnZ = augcc-pVnZ (n = D, T, Q)

and includes the D3 [56] empirical dispersion correction. It has been shown to perform well for a wide range of systems [53]. In the present study, we also find it to perform well for the barriers for hydrogen-atom-abstraction reactions.

For the wavefunction methods, we find a surprisingly good performance by MP2, which somewhat fortuitously produces MADs similar to those for the much more costly MP4 or CCSD. At the intermediate MP3 level, the MADs are larger than for MP2, MP4, and CCSD. We also note that CCSD yields somewhat larger MADs than MP4 and MP2. For all wavefunction methods examined, there is a consistent basis set effect, in which a larger basis set generally leads to a lower MAD. We find that R performs slightly better than U. We also note that for URCCSD(T), there is a difference of 1.8 kJ mol⁻¹ between the MAD for aug-cc-pVTZ and that for aug-cc-pVQZ.

Table 5 Mean absolute deviations from URCCSD(T)/AVQZ^a benchmark values for vibrationless reaction energies (kJ mol⁻¹) for reactions 1 and $6-10^{b}$

	B1	B2	B3	B4	LXP	VDZ	VTZ	VQZ	AVDZ	AVTZ	AVQZ
Pure DFT methods											
B-LYP	31.2	7.4	7.0	7.4	7.0	18.4	8.7	7.1	6.8	6.5	6.8
M06-L	31.5	14.3	15.1	15.0	14.2	23.5	17.2	17.6	13.7	15.0	17.0
Hybrid DFT metho	ds										
B3-LYP	34.6	9.9	7.4	5.7	5.6	19.7	9.8	7.1	4.7	5.7	5.5
LC-B-LYP	33.9	10.3	7.8	7.2	7.6	18.0	7.0	7.6	8.0	7.8	8.0
CAM-B3-LYP	35.7	10.7	6.4	4.7	4.6	20.3	8.8	6.0	3.6	4.7	4.5
ωB97X-D	34.8	0.1	8.4	7.2	6.8	20.5	11.1	8.8	6.1	7.7	7.5
BH&H-LYP	42.1	17.9	14.1	11.6	11.5	26.3	15.9	13.1	11.6	12.2	11.7
BMK	38.8	15.3	10.9	8.8	8.7	23.9	12.7	11.8	8.4	9.6	10.6
M05	30.5	7.8	8.9	10.7	10.6	21.5	11.7	10.2	8.7	8.6	9.3
M05-2X	33.1	8.5	6.5	4.3	4.2	18.8	6.2	5.1	3.4	3.3	4.0
M06	29.0	6.8	5.5	6.0	5.7	15.5	8.6	7.1	4.3	5.1	5.7
M06-2X	35.6	11.7	7.5	5.8	5.8	19.9	8.5	7.1	4.4	5.1	5.8
Double-hybrid DF	T methods										
UB2-PLYP	37.1	11.8	6.7	3.3	3.5	21.9	8.7	4.5	3.7	3.4	2.6
UB2K-PLYP	38.4	13.5	7.8	4.3	4.6	23.1	9.3	5.0	5.1	3.5	2.4
RB2-PLYP	37.5	11.6	5.6	2.0	2.3	21.9	7.7	3.3	3.3	2.3	1.8
RB2K-PLYP	38.0	12.4	6.3	3.3	3.6	22.3	7.4	3.9	5.6	3.5	2.0
UB2-PLYP-09	37.5	12.3	6.9	3.3	3.5	22.2	8.6	4.3	4.0	2.9	2.0
ROB2-PLYP	38.9	13.1	6.9	3.3	3.6	23.1	8.7	4.4	4.8	3.2	3.1
DSD-B-LYP-D3	37.9	12.8	7.1	3.6	3.9	22.7	8.7	4.2	4.5	2.6	2.3
Unrestricted wavef	unction me	thods									
UHF	52.0	29.1	27.4	25.1	25.6	35.9	28.3	26.5	25.1	26.3	25.8
UMP2	35.0	18.6	15.7	16.4	16.7	20.3	13.5	15.9	15.7	16.2	17.1
UMP3	37.9	19.5	13.6	10.7	11.1	24.8	13.3	9.0	11.9	10.1	7.8
UMP4	41.5	18.2	12.2	8.7	9.1	26.8	11.7	6.9	10.0	7.7	6.6
UCCSD	36.9	14.7	10.6	7.2	7.7	23.0	10.0	4.9	6.8	5.7	2.7
UCCSD(T)	37.6	14.7	9.7	5.6	6.1	23.3	8.7	3.1	5.6	3.7	0.3
Restricted-open-she	ell wavefun	ction meth	ods								
RHF	57.8	33.6	29.6	27.0	27.3	41.3	30.8	28.5	28.7	28.1	27.6
RMP2	30.6	13.6	10.8	11.4	11.8	15.8	8.5	10.3	11.0	10.7	11.1
RMP3	35.8	18.1	12.4	9.5	9.9	22.7	12.1	7.7	10.5	8.8	6.3
RMP4	37.7	14.6	8.6	5.1	5.6	23.1	8.0	3.1	6.4	4.1	3.3
URCCSD	37.1	15.0	10.7	7.3	7.8	23.2	10.1	5.0	7.1	5.9	3.0
URCCSD(T)	37.5	14.6	9.4	5.4	5.9	23.1	8.4	2.8	5.4	3.5	0.0

^a The aug-cc-pwCVQZ basis set was employed for bromine

^b B1 = 6-31G(d), B2 = 6-31+G(d,p), B3 = 6-311+G(2df,p), B4 = 6-311+G(3df,2p), LXP = G3LargeXP, VnZ = cc-pVnZ, AVnZ = augcc-pVnZ (n = D, T, Q)

Turning our attention to the performance of the various methods in calculating reaction energies (Table 5), we find that the use of the 6-31G(d) basis set leads to substantial deviations from the URCCSD(T)/aug-cc-pVQZ values, with MADs in excess of 30 kJ mol⁻¹ for all methods. In addition, the use of the cc-pVDZ basis set gives double-digit deviations for all methods, while calculations using 6-31+G(d,p) also give substantial MADs. When an appropriate basis set is

used, most DFT procedures give MADs that are smaller than 10 kJ mol⁻¹. Two notable exceptions are the M06-L and the BH&H-LYP functionals, which substantially overestimate the reaction energies. Thus, while BH&H-LYP provides fair estimations of the geometries of the transition structures, it does not give a good account for the reaction energies. On the basis of the performance for reaction energies as well as that for barriers, we find M05-2X to be an adequately reliable

hybrid functional for the study of hydrogen-abstraction reactions.

The UB2-PLYP, RB2-PLYP, UB2K-PLYP, RB2K-PLYP, UB2-PLYP-09, ROB2-PLYP, and DSD-B-LYP-D3 double-hybrid functionals all perform comparably for reaction energies. In this case, a systematic improvement with increasing basis set size is observed for all methods. As is the case for the calculated barriers, we find only minor differences when comparing the performance of U and R formalisms. Taking the observations for both the barriers and reaction energies into account, we deem the use of UB2K-PLYP, RB2K-PLYP, UB2-PLYP-09, ROB2-PLYP, and DSD-B-LYP-D3 in combination with an augmented triple-zeta-quality basis set an appropriate methodology for studying the energies of these types of hydrogen-abstraction reactions.

For the wavefunction methods, MP2 is found to be less good for reaction energies than for barriers. It also displays a non-monotonic basis set effect. For the MP series, when used in combination with reasonably sized basis sets, there is generally a consistent improvement in the performance with increasing electron correlation, with the MADs decreasing in the order MP2 > MP3 > MP4. We find that URCCSD outperforms UMP4 but URCCSD gives somewhat larger MADs than RMP4.

It is noteworthy that, in general, a consistent basis set effect is found in calculating reaction energies for the correlation methods beyond MP2. We note that aug-ccpVDZ outperforms cc-pVTZ and that aug-cc-pVTZ yields MADs comparable to cc-pVQZ. Thus, it appears that the inclusion of diffuse functions is required to obtain reliable energies for these reactions. We also note that there is a 5.4 kJ mol^{-1} difference between the calculated reaction energies for URCCSD(T) with the aug-cc-pVDZ and the aug-cc-pVQZ basis sets, and a 3.5 kJ mol^{-1} difference between the aug-cc-pVQZ values. This further highlights the importance of employing an adequately sized basis set for studying these reactions. Finally we note that as is the case for the barriers, there is only a minor difference between reaction energies obtained with U and R formalisms for highly correlated procedures.

3.3 The reaction of CH₃CHO

The reaction of Cl• with CH₃CHO to give ClH and •CH₂CHO (reaction 10) has been previously identified to be a challenging case for theoretical methods due to high spin contamination in the transition structure and in the product radical [22]. Indeed, the transition structure and the •CH₂CHO radical have the largest $\langle S^2 \rangle$ values among all species examined, specifically 0.90 and 0.92, respectively, at the UHF/aug-cc-pVQZ level, which are substantially larger than the value of 0.75 for a pure doublet state. We have therefore examined in greater detail the barrier and reaction energy for this reaction obtained with unrestricted and restricted-open-shell procedures (Table 6).

Table 6 Differences in barriers and reaction energies calculated with unrestricted and restricted-open-shell methods for $Cl \bullet + CH_3CHO \rightarrow ClH + \bullet CH_2CHO$ (U–R, kJ mol⁻¹)

	B1	B2	B3	B4	LXP	VDZ	VTZ	VQZ	AVDZ	AVTZ	AVQZ
Barrier											
B2-PLYP	-3.1	-3.0	-2.8	-2.5	-2.7	-2.9	-2.0	-1.8	-2.7	-1.9	-1.9
B2K-PLYP	-2.7	-2.7	-3.3	-3.3	-3.8	-2.5	-1.6	-1.4	-3.7	-1.8	-1.7
HF	-27.8	-26.4	-23.0	-22.7	-22.2	-26.2	-23.0	-22.5	-24.4	-22.4	-22.4
MP2	32.4	31.0	31.5	31.4	31.4	31.4	31.8	32.5	30.2	31.8	32.6
MP3	14.9	13.4	12.4	12.2	12.2	13.9	12.5	12.8	12.7	12.4	12.9
MP4	18.9	17.9	17.8	18.2	18.2	18.2	18.1	19.2	17.6	18.8	19.2
CCSD	-0.8	-0.9	-0.8	-0.8	-0.7	-0.8	-0.8	-0.7	-0.9	-0.8	-0.7
CCSD(T)	1.0	1.0	1.4	1.4	1.5	1.1	1.4	1.5	1.1	1.5	2.1
Reaction ener	·gy										
B2-PLYP	-1.6	-1.3	-0.6	-0.5	-0.5	-1.5	-0.3	-0.1	-1.3	0.7	0.9
B2K-PLYP	0.5	1.0	0.9	1.0	1.1	0.4	1.6	2.0	0.7	-1.3	-1.2
HF	-31.3	-29.0	-25.0	-24.8	-24.1	-31.3	-26.0	-24.9	-27.2	-24.6	-24.5
MP2	32.5	32.5	32.3	32.4	32.3	31.1	32.4	33.3	31.4	32.9	33.7
MP3	11.7	10.9	9.1	9.2	9.1	9.9	9.2	9.7	10.0	9.4	9.9
MP4	21.2	20.9	20.3	20.5	20.6	20.4	21.2	22.2	19.8	20.9	21.3
CCSD	-1.8	-1.7	-1.7	-1.7	-1.6	-2.0	-1.8	-1.7	-1.7	-1.7	-1.6
CCSD(T)	0.6	0.6	1.1	1.2	1.3	0.8	1.2	1.3	0.9	1.2	1.3

B1 = 6-31G(d), B2 = 6-31+G(d,p), B3 = 6-311+G(2df,p), B4 = 6-311+G(3df,2p), LXP = G3LargeXP, VnZ = cc-pVnZ, AVnZ = aug-cc-pVnZ (n = D, T, Q)

We can see that for the B2-PLYP and B2K-PLYP double-hybrid DFT procedures, there are only small differences in the barriers and reaction energies calculated with U and R formalisms. This is consistent with previous findings from Menon et al. for C-H BDEs, where there are only very minor U-R differences [57]. In contrast, the U-R values for wavefunction methods are substantial, until one reaches the CCSD or CCSD(T) levels. It is apparent that UHF gives lower barriers and reaction energies than RHF, as indicated by the negative U-R values. This is consistent with the larger variational freedom for UHF than for RHF. However, UMP2, UMP3, and UMP4 all yield barriers and reaction energies that are higher than those for the corresponding R counterparts, with MP2 giving the largest U-R values while MP3 yields the smallest. For the MP series, we find that R procedures give closer agreement with the benchmark URCCSD(T)/aug-cc-pVQZ values (supplementary material, Tables S2 and S3). When reaction 10 is excluded from our analysis, we find that U and R formalisms perform very similarly to one another (supplementary material, Tables S4 and S5).

4 Concluding remarks

In this study, we have examined a number of hydrogenabstraction reactions and assessed a number of DFT procedures for their performance for geometry optimization and the performance of various DFT and wavefunction methods for calculating relative energies. The following major findings emerge from the present study:

- The BH&H-LYP and M05-2X procedures with the 6-31+G(d,p) basis set provide reasonable predictions for the geometries of the transition structures for hydrogen-atom abstraction by chlorine atom. They also yield reasonable imaginary frequencies when compared with the benchmark values, which is indicative of good descriptions of the potential energy surfaces near the saddle points.
- Despite being reasonably accurate in predicting geometries, the BH&H-LYP functional does not give rise to good barriers or reaction energies for the prototypical abstraction reactions examined. On the other hand, we find that the M05-2X functional, when combined with adequate basis sets, provides a reasonably accurate and cost-effective estimate of barriers and reaction energies.
- We find that double-hybrid functionals, when used with suitable basis sets, yield close agreement with the benchmark URCCSD(T) energies. The basis set effect for these functionals depends on the proportion of wavefunction methods in the procedures. At the

extremes, B2K-PLYP, with a large proportion of HF exchange and MP2 correlation, displays a performance that is rather sensitive to basis set size, while the behavior of B2-PLYP is less dependent on the size of the basis set. We recommend the use of B2K-PLYP, UB2-PLYP-09, ROB2-PLYP, and DSD-B-LYP-D3 with an augmented triple-zeta quality basis set for studying these reactions.

• For wavefunction methods, we find that it is important to use the high-level CCSD(T) procedure in combination with a diffuse-function-augmented basis set that is preferably of triple-zeta quality for an accurate account of both the barriers and the reaction energies for the hydrogen-abstraction reactions. We find that the use of either U or R reference wavefunctions yields very similar results, except in the case of abstraction from CH₃CHO, where high spin contamination in the transition structure and the radical product leads to substantially different UHF and UMP*n* values compared with the R counterparts. In this case, the R formalism yields results that are in better agreement with the benchmark.

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